

PREHĽAD VZŤAHOV

Mocniny:

$$a^x \cdot a^y = a^{x+y} \quad \frac{a^x}{a^y} = a^{x-y} \quad (a^x)^y = a^{x \cdot y} \quad (a \cdot b)^x = a^x \cdot b^x \quad \left(\frac{a}{b}\right)^x = \frac{a^x}{b^x} \quad a^{-x} = \frac{1}{a^x} \quad a^{\frac{x}{y}} = \sqrt[y]{a^x}$$

Goniometrické funkcie:

$$\sin^2 x + \cos^2 x = 1 \quad \operatorname{tg} x = \frac{\sin x}{\cos x}$$

$$\sin 2x = 2 \cdot \sin x \cos x \quad \cos 2x = \cos^2 x - \sin^2 x$$

$$\sin\left(\frac{\pi}{2} - x\right) = \cos x \quad \cos\left(\frac{\pi}{2} - x\right) = \sin x$$

| | | | | | |
|-------|----|----------------------|----------------------|----------------------|-----------------|
| | 0 | $\frac{\pi}{6}$ | $\frac{\pi}{4}$ | $\frac{\pi}{3}$ | $\frac{\pi}{2}$ |
| | 0° | 30° | 45° | 60° | 90° |
| sin x | 0 | $\frac{1}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{3}}{2}$ | 1 |
| cos x | 1 | $\frac{\sqrt{3}}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{1}{2}$ | 0 |

Trigonometria: Sínusová veta: $\frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma} = 2r$ Kosínusová veta: $c^2 = a^2 + b^2 - 2ab \cdot \cos \gamma$

Logaritmus: $\log_z(x \cdot y) = \log_z x + \log_z y$ $\log_z \frac{x}{y} = \log_z x - \log_z y$

$$\log_z x^k = k \cdot \log_z x \quad \log_y x = \frac{\log_z x}{\log_z y}$$

Aritmetická postupnosť: $a_n = a_1 + (n-1) \cdot d$ $s_n = \frac{n}{2} (a_1 + a_n)$

Geometrická postupnosť: $a_n = a_1 \cdot q^{n-1}$ $s_n = a_1 \frac{q^n - 1}{q - 1}, q \neq 1$

Kombinatorika: $P(n) = n!$ $V(k, n) = \frac{n!}{(n-k)!}$ $C(k, n) = \binom{n}{k} = \frac{n!}{(n-k)! k!}$

$$P'(n_1, n_2, \dots, n_k) = \frac{n!}{n_1! n_2! \dots n_k!} \quad V'(k, n) = n^k \quad C'(k, n) = \binom{n+k-1}{k}$$

Analytická geometria: Parametrické vyjadrenie priamky: $X = A + t\vec{u}, t \in R$

Všeobecná rovnica priamky: $ax + by + c = 0; [a; b] \neq [0; 0]$

Uhol vektorov: $\cos \varphi = \frac{\vec{u} \cdot \vec{v}}{|\vec{u}| \cdot |\vec{v}|}$

Vzdialenosť bodu $M[m_1; m_2]$ od priamky $p: ax + by + c = 0$: $|Mp| = \frac{|am_1 + bm_2 + c|}{\sqrt{a^2 + b^2}}$

Stredový tvar rovnice kružnice: $(x - m)^2 + (y - n)^2 = r^2$

Objemy a povrchy telies:

| | | | | | |
|--------|-------------------|-----------------------|---------------------|-------------------------|-----------------------|
| | kváder | valec | ihlan | kužeľ | guľa |
| objem | abc | $\pi r^2 v$ | $\frac{1}{3} S_p v$ | $\frac{1}{3} \pi r^2 v$ | $\frac{4}{3} \pi r^3$ |
| povrch | $2(ab + ac + bc)$ | $2\pi r^2 + 2\pi r v$ | $S_p + S_{pl}$ | $\pi r^2 + \pi r s$ | $4\pi r^2$ |